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# **SHAtrop: the new tropospheric delay model over China continent**

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# *Content*

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- **Background**
- **SHAtrop: ZTD Modeling**
- **SHAtrop: ZTD Grid modeling**
- **SHAtrop: Model validation**
- **Summary**

# *Troposphere modeling*

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## ➤ Slant Propagation Delay

$$SPD(e) = Z_h \bullet MF_h(e) + Z_w \bullet MF_w(e)$$

$$ZTD = Z_h + Z_w, \quad e = 90^\circ$$

## ➤ ZTD:

- EGNOS/UNB3 et al
- Saastamoinen/Hopfield et al using :
  - weather data at the site
  - numerical weather model (NWM)
  - empirical pressure/temperature model (GPT2/GPT2w)
- Ray-traced delays (VMF1/UNB-VMF)
- **Empirical model based on GNSS ZTD**

# SHAtrop: *overview*

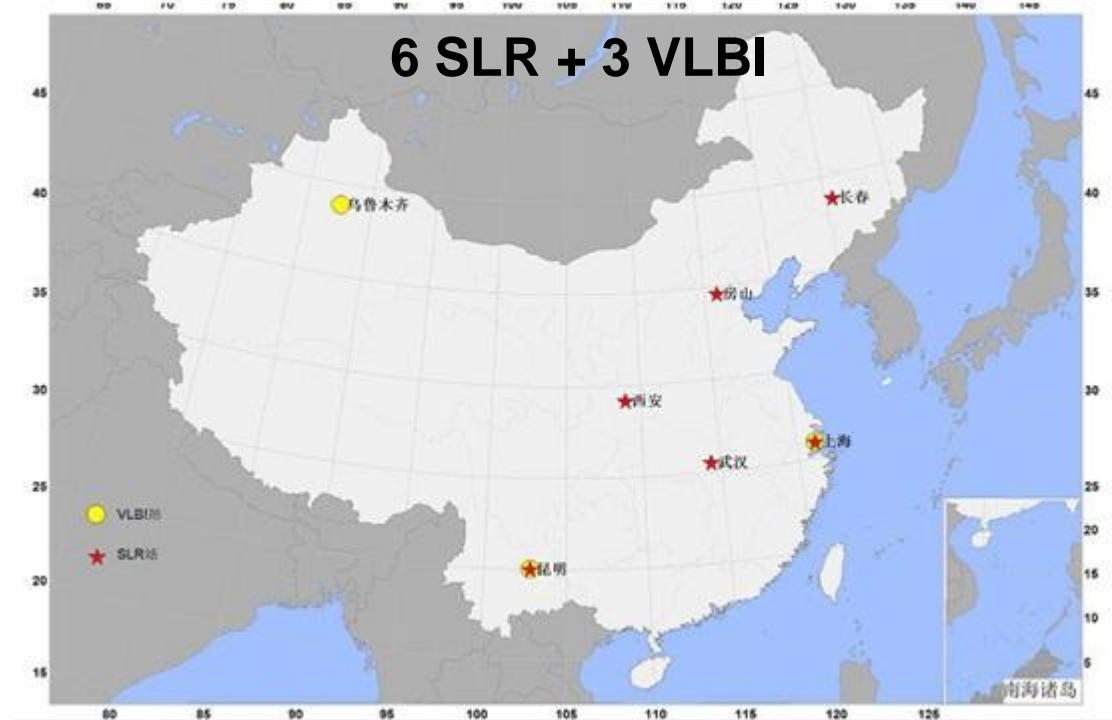
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- Empirical regional ZTD model over China continent
- GNSS ZTD estimates (of 223 continuous GNSS sites) at Shanghai Astronomical Observatory
- ZTD is modeled by a function of station height and the ZTD at geoidal surface (ZTD-Geiod).
- Grid model with high spatial resolution ( $2^\circ \times 2.5^\circ$  )
- Without weather data, easy to implement

# SHAtrop: *data*

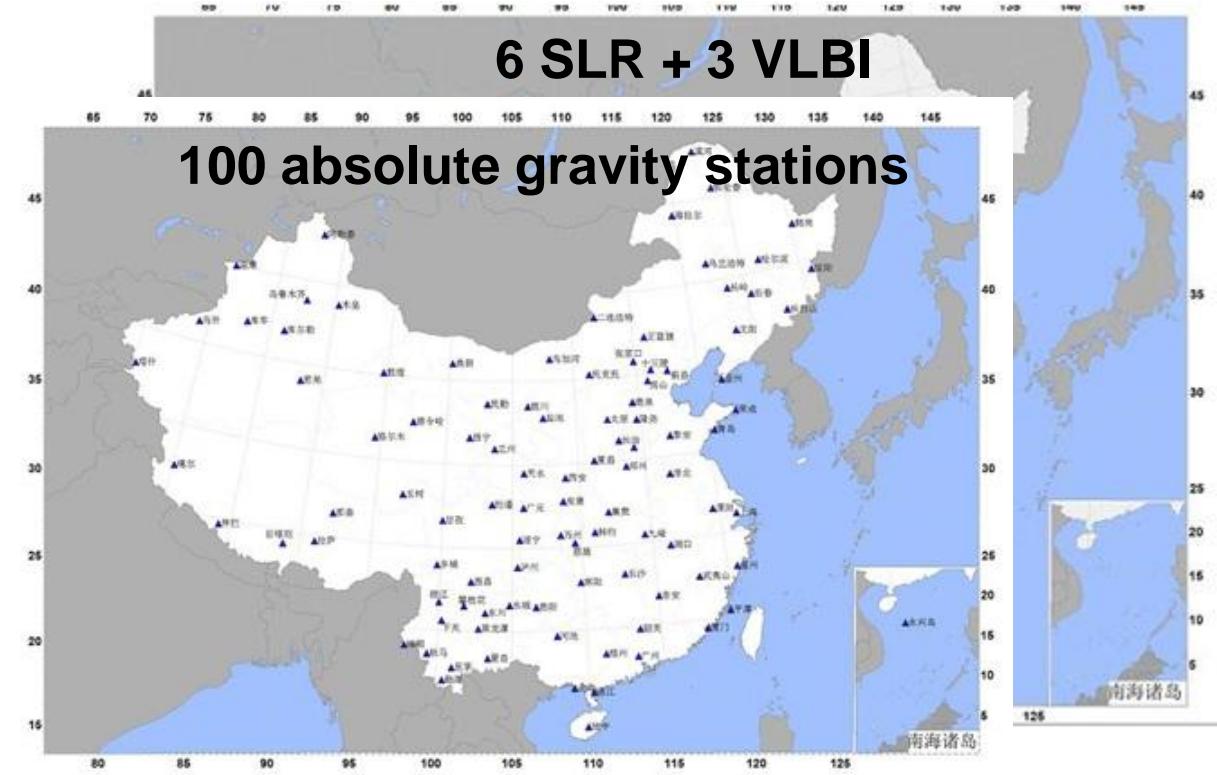
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➤ CMONOC (Crustal Movement Observation Network of China)



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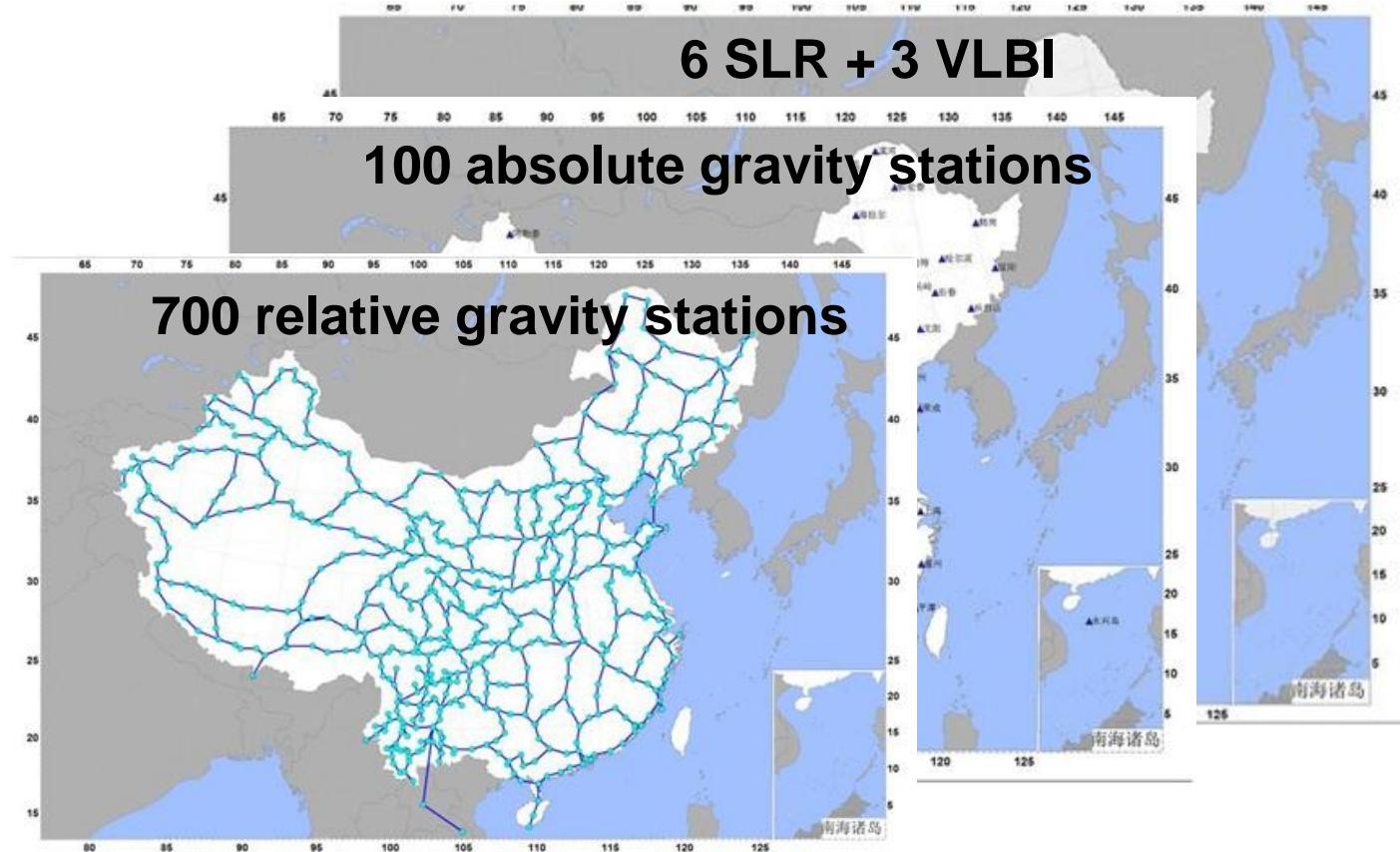
➤ CMONOC (Crustal Movement Observation Network of China)



<http://neiscn.org/>

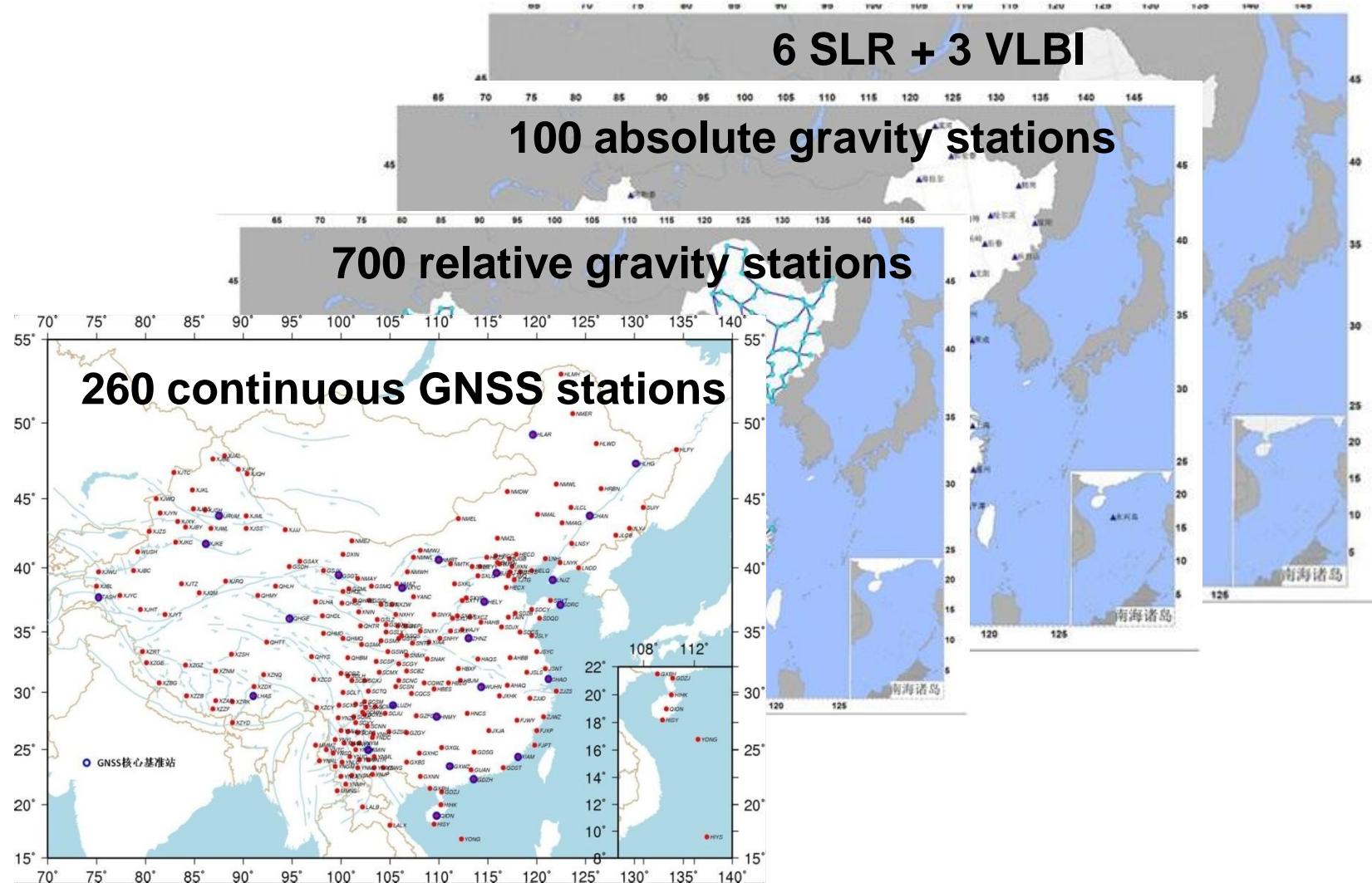
# SHAtrop: *data*

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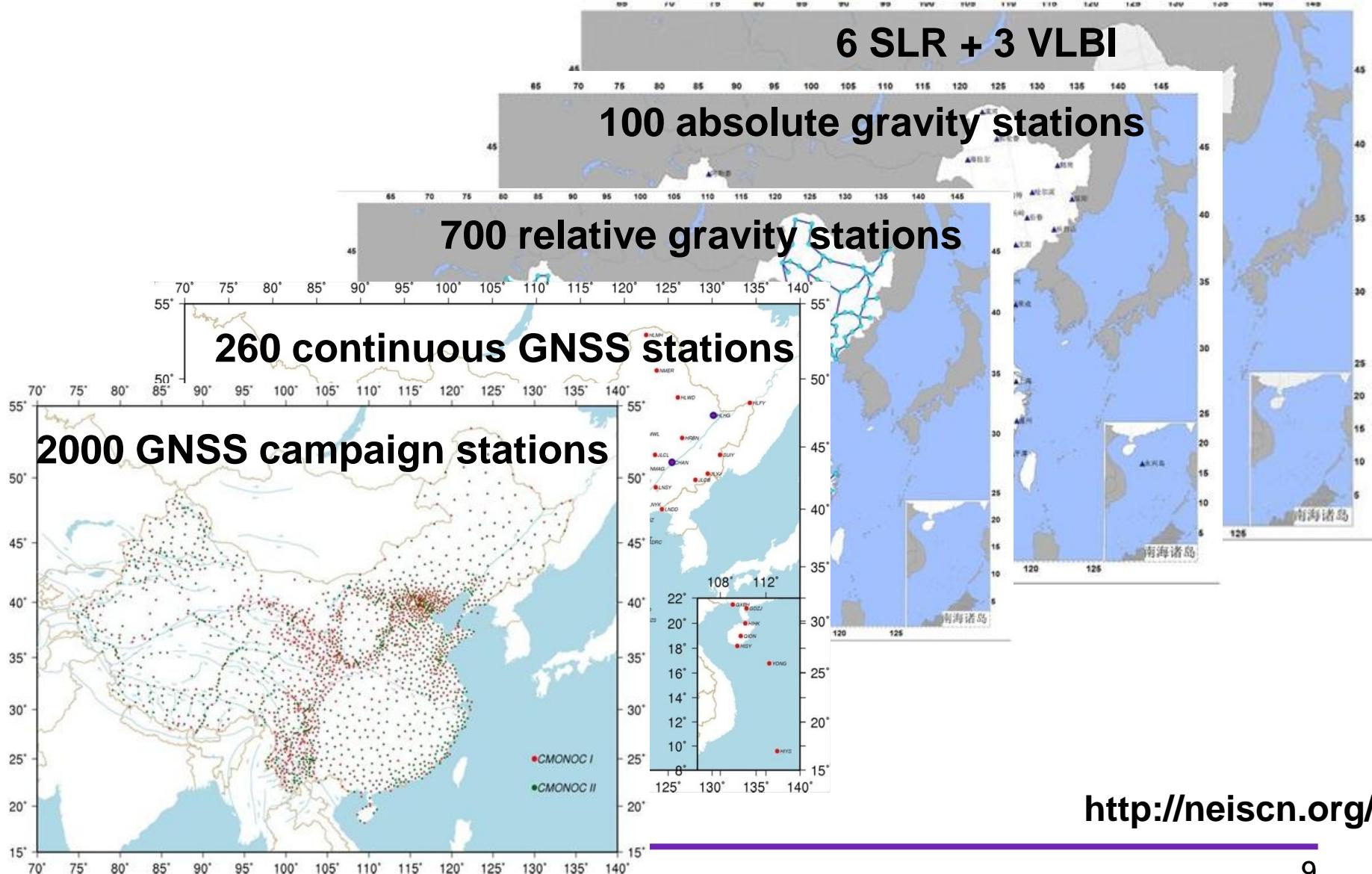
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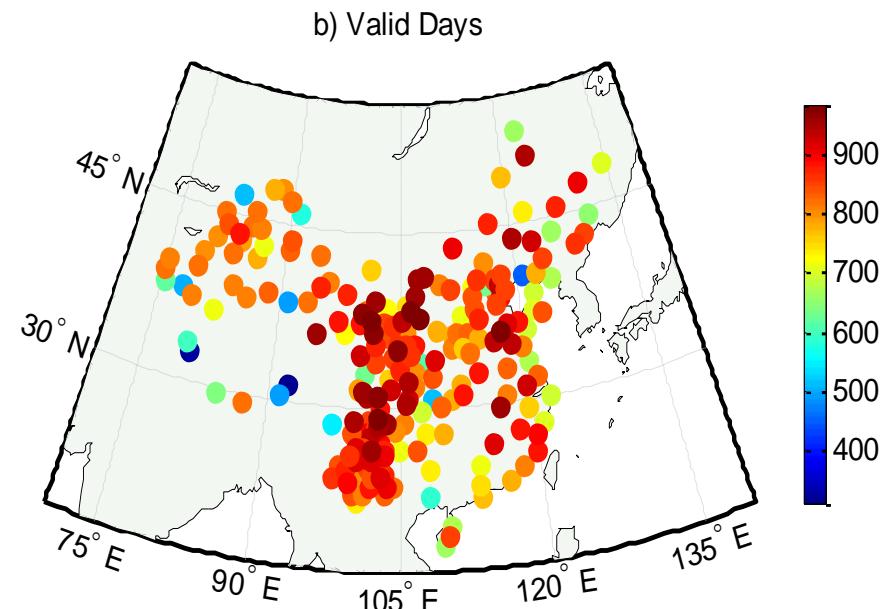
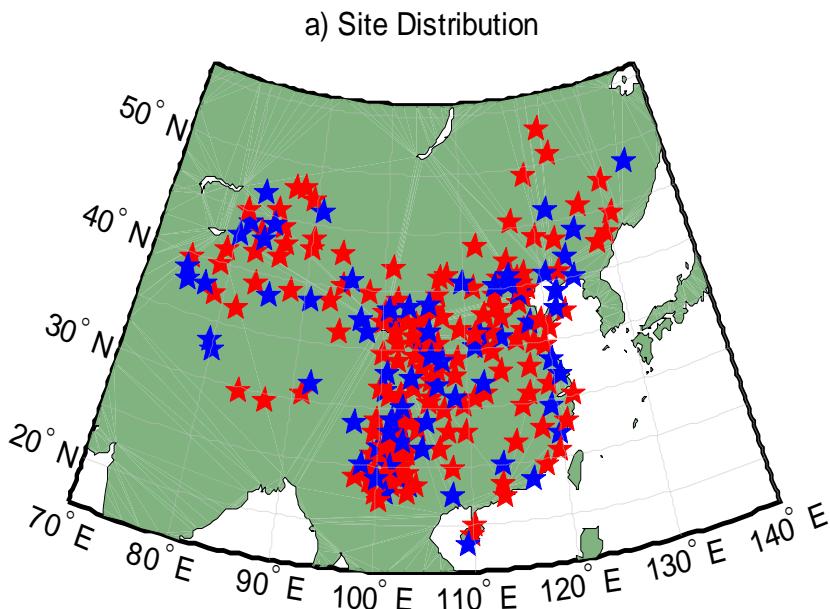
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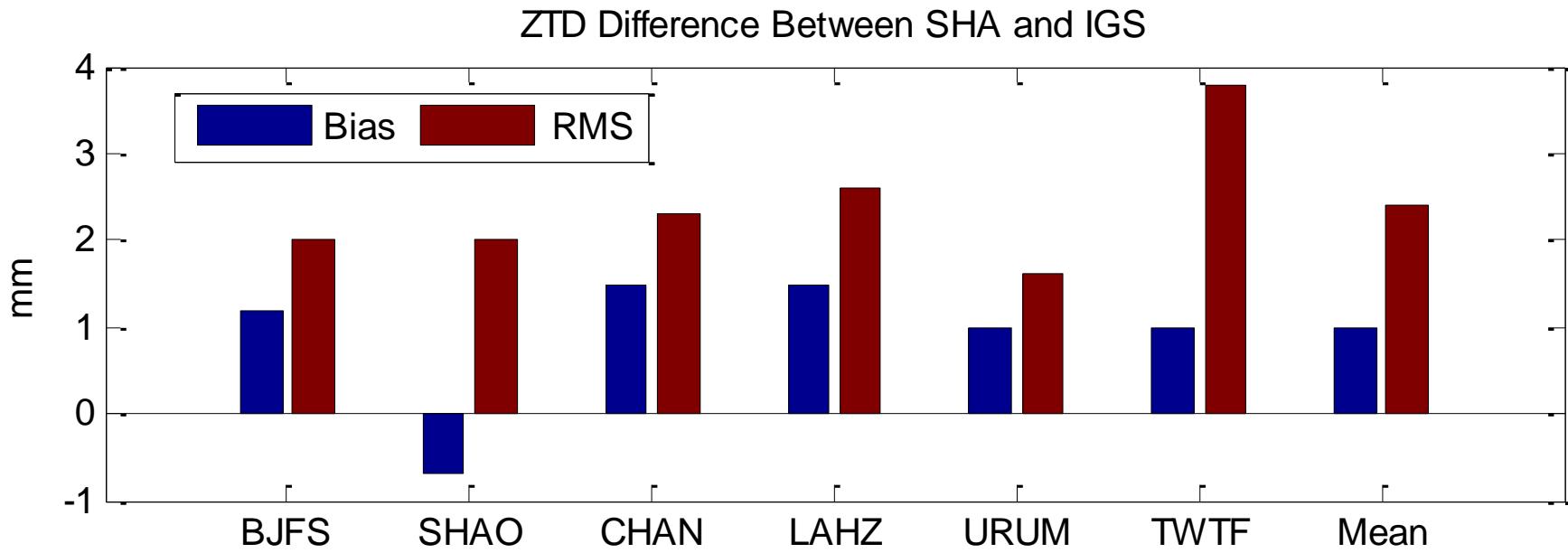
- 4 years' GNSS ZTD estimates (of 223 continuous GNSS sites) at Shanghai Astronomical Observatory;
- Model determination: 152; model validation: 152+71;
- Spanning: 2012-2014



# SHAtrop: *data*

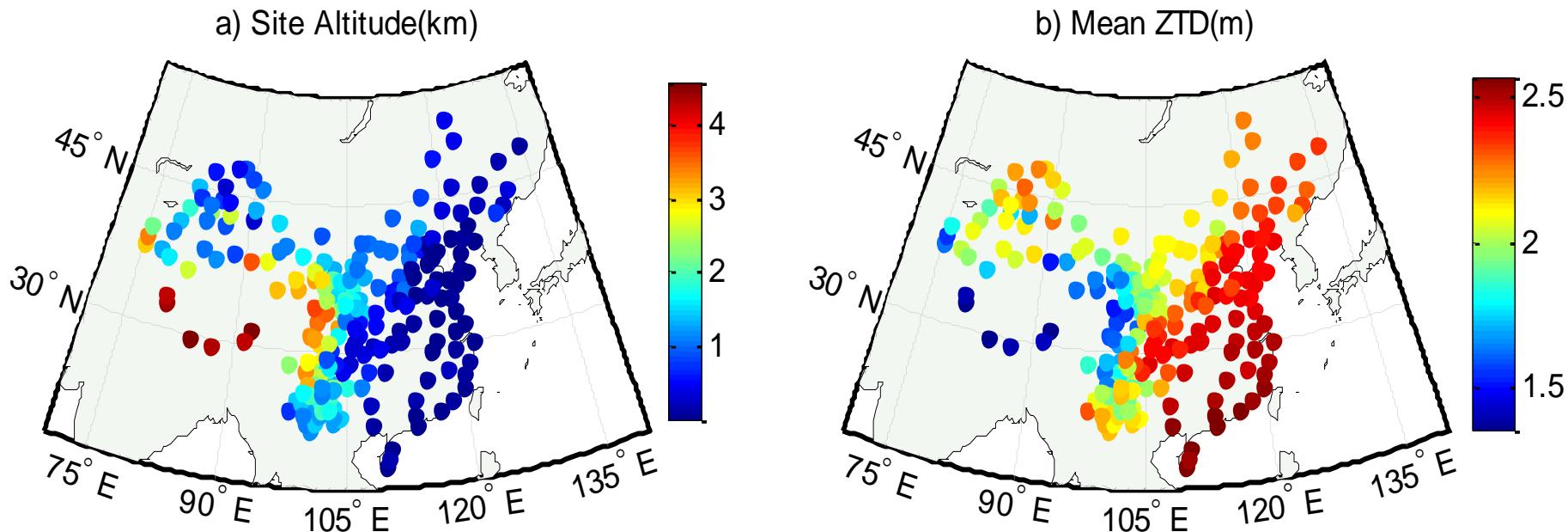
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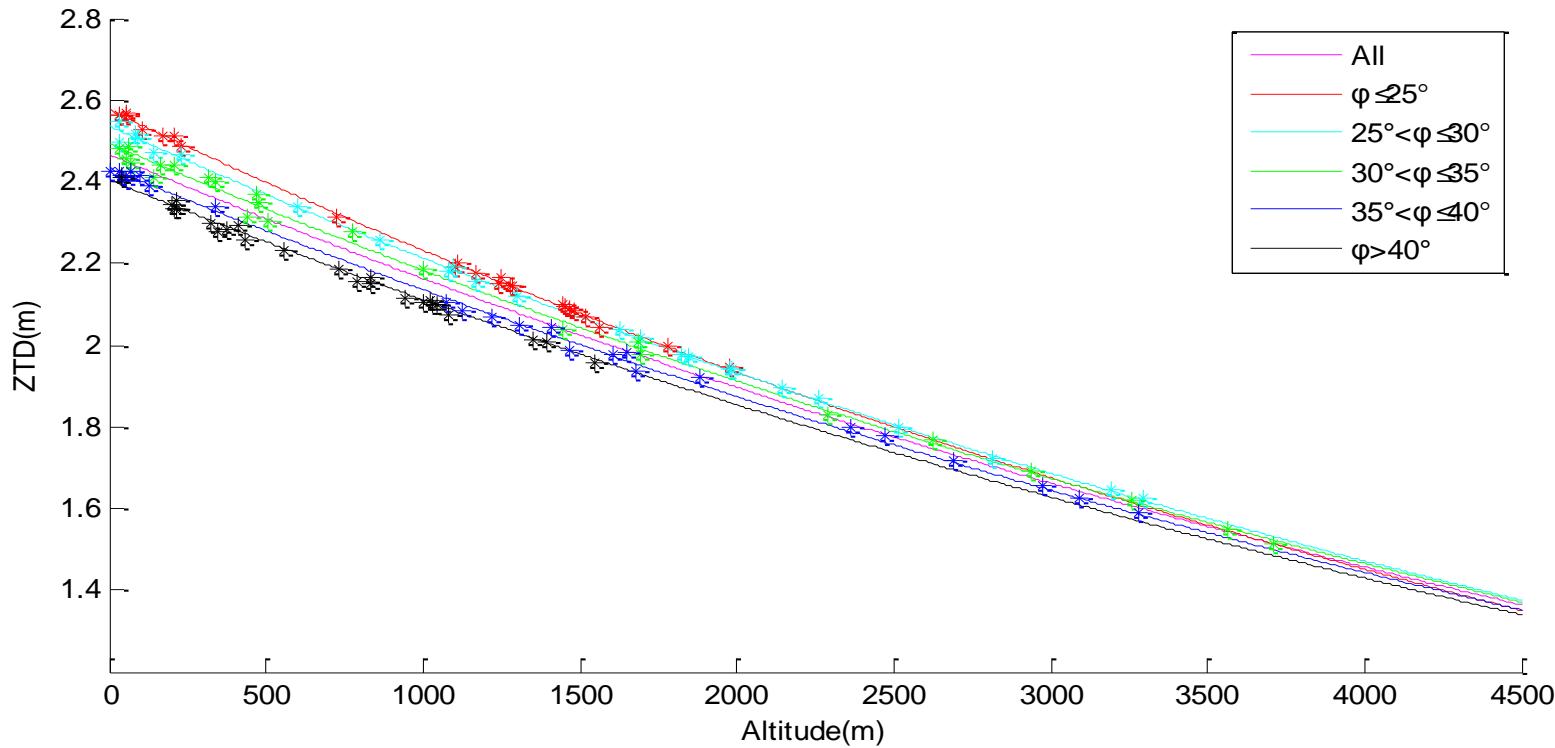
# SHAtrop: ZTD v.s. station height

- Mean annual ZTD with respect to station height



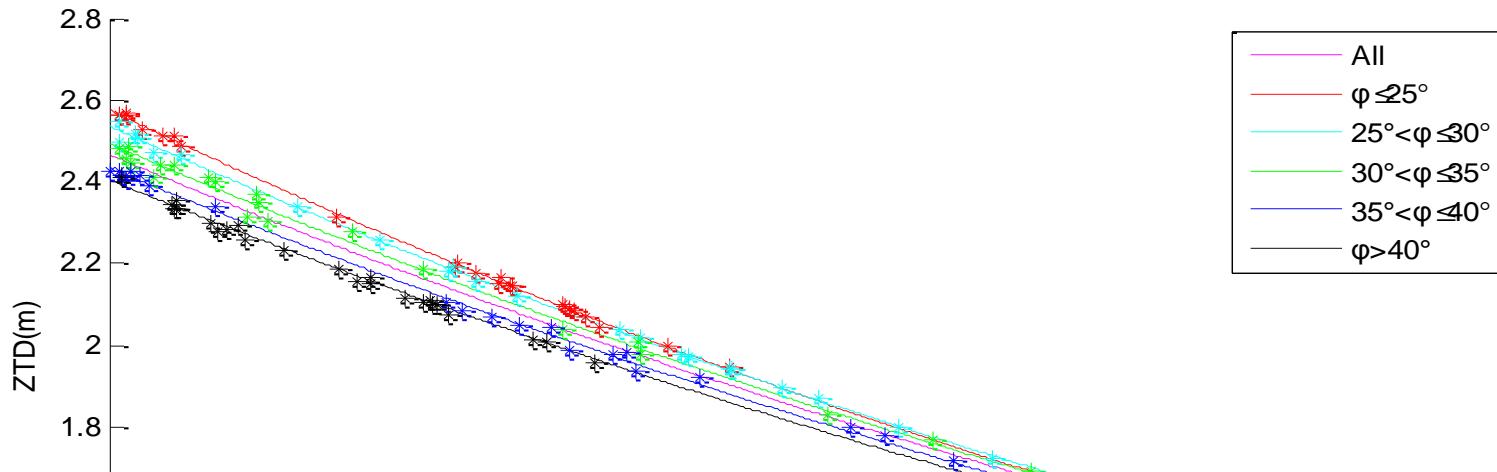
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- Fitting of annual ZTD with respect to station height:  $\beta$  varies with station latitude



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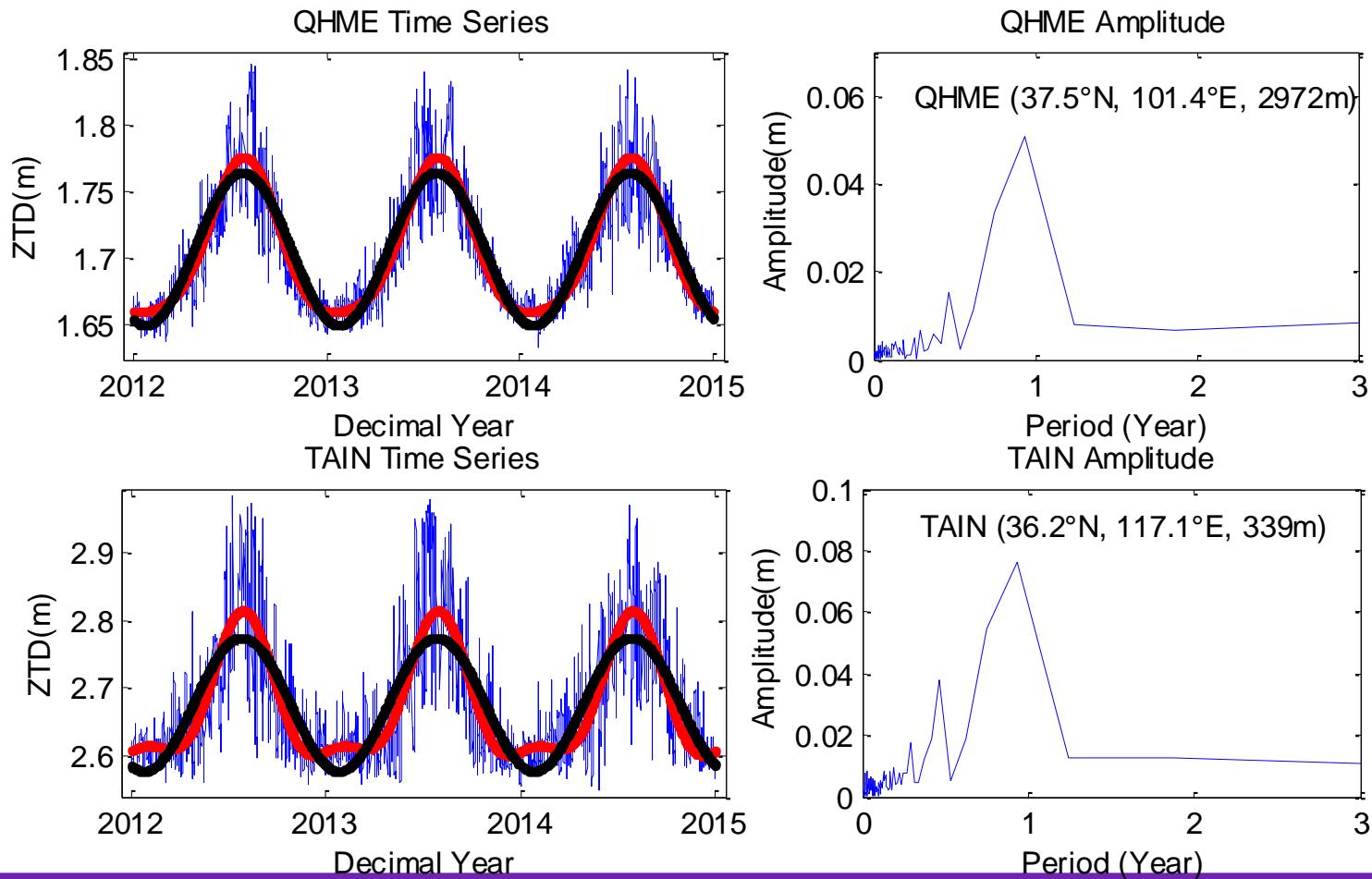


$$ZTD(h) = ZTD_0 \times e^{\beta h}$$

Latitude	$< 25^\circ$ N	$25^\circ$ N~ $30^\circ$ N	$30^\circ$ N~ $35^\circ$ N	$35^\circ$ N~ $40^\circ$ N	$> 40^\circ$ N
$\beta (10^{-3})$	- 0.1435	- 0.1359	- 0.1329	- 0.1306	- 0.1300

# SHAtrop: ZTD period term

- ZTD time series fitting with annual and semi-annual terms
- amplitude derived from fast Fourier transform



# SHAtrop: ZTD model over China continent

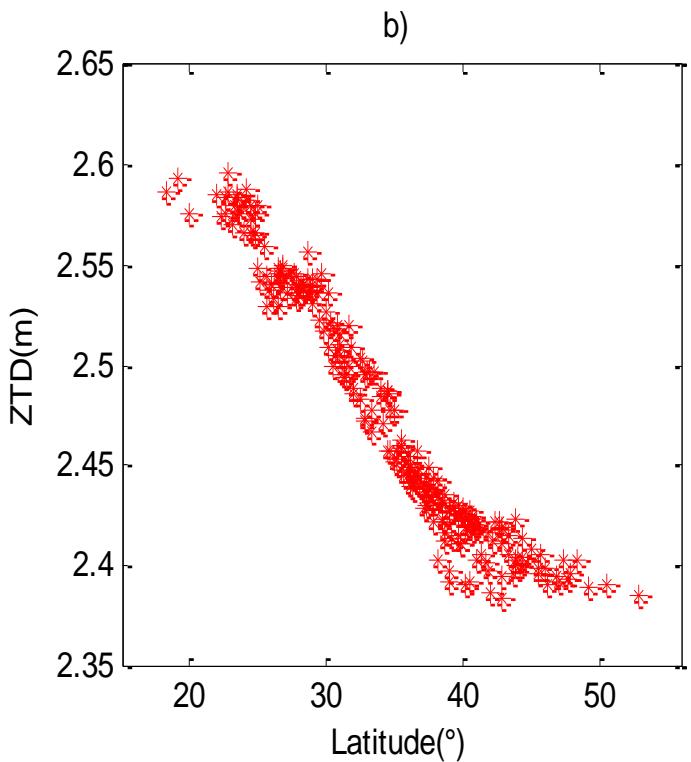
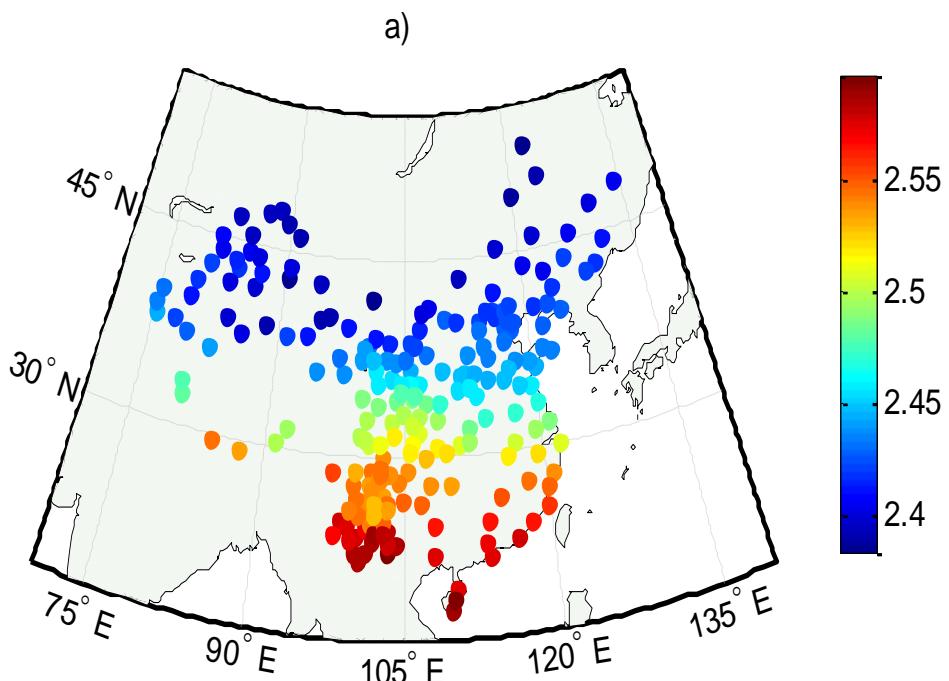
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- ZTD modeled with function of station height over Geoid (constant term) and periodical terms

$$ZTD(doy) = ZTD_m + A_1 \cos\left(\frac{2\pi}{365.25}(doy - d_1)\right) + A_2 \cos\left(\frac{4\pi}{365.25}(doy - d_2)\right)$$

# SHAtrop: ZTD constant term

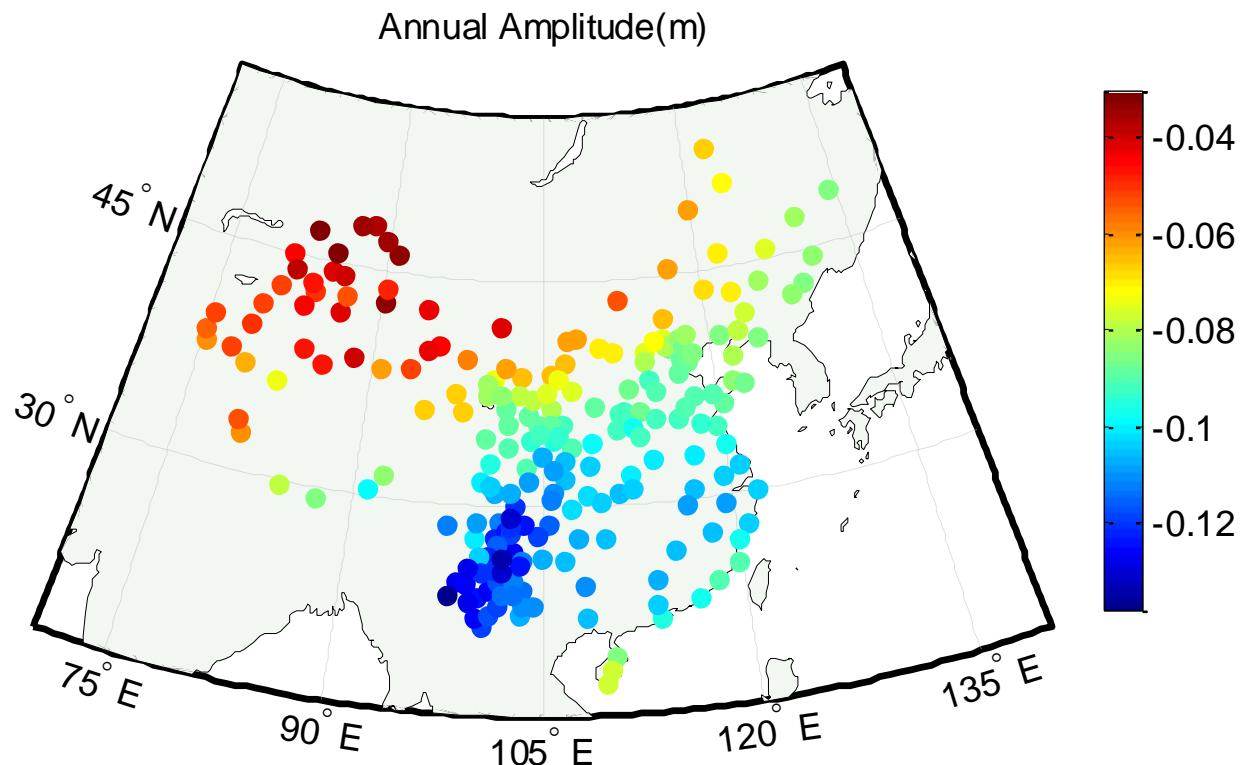
- Constant term of all sites
- Constant term v.s. site latitude



# SHAtrop: ZTD annual term

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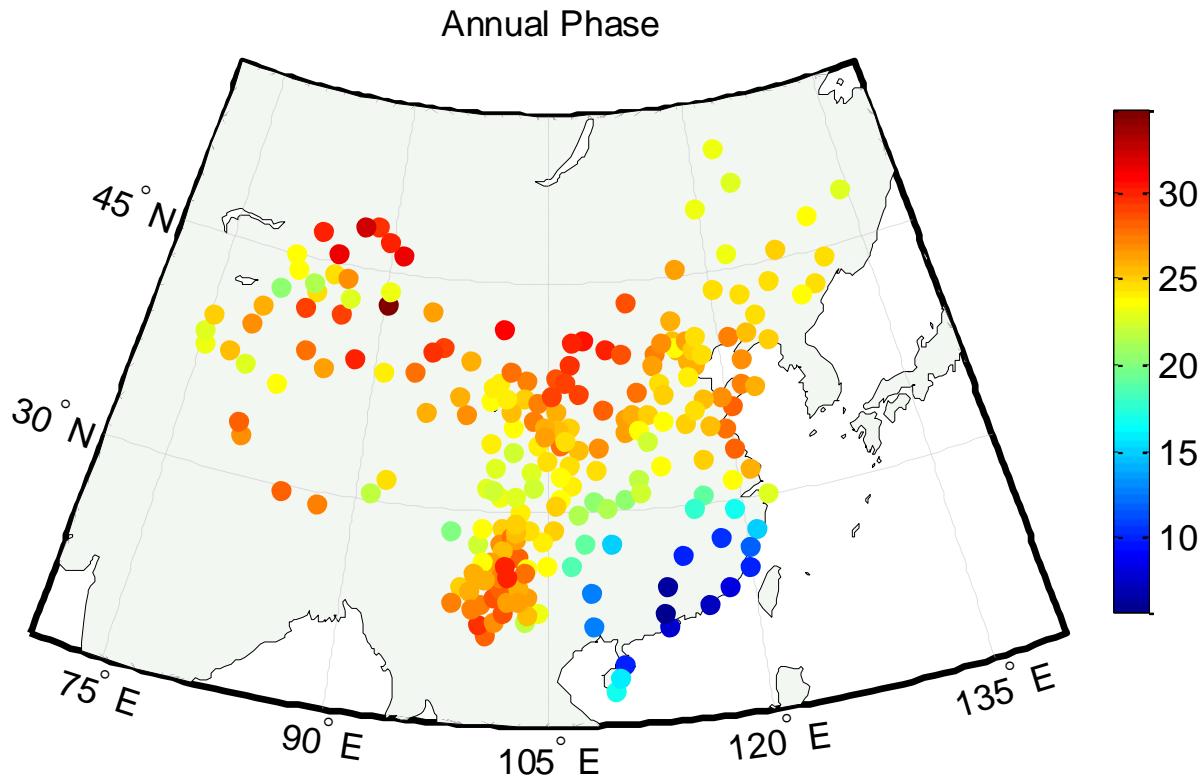
## ➤ Annual amplitude



# SHAtrop: ZTD annual term

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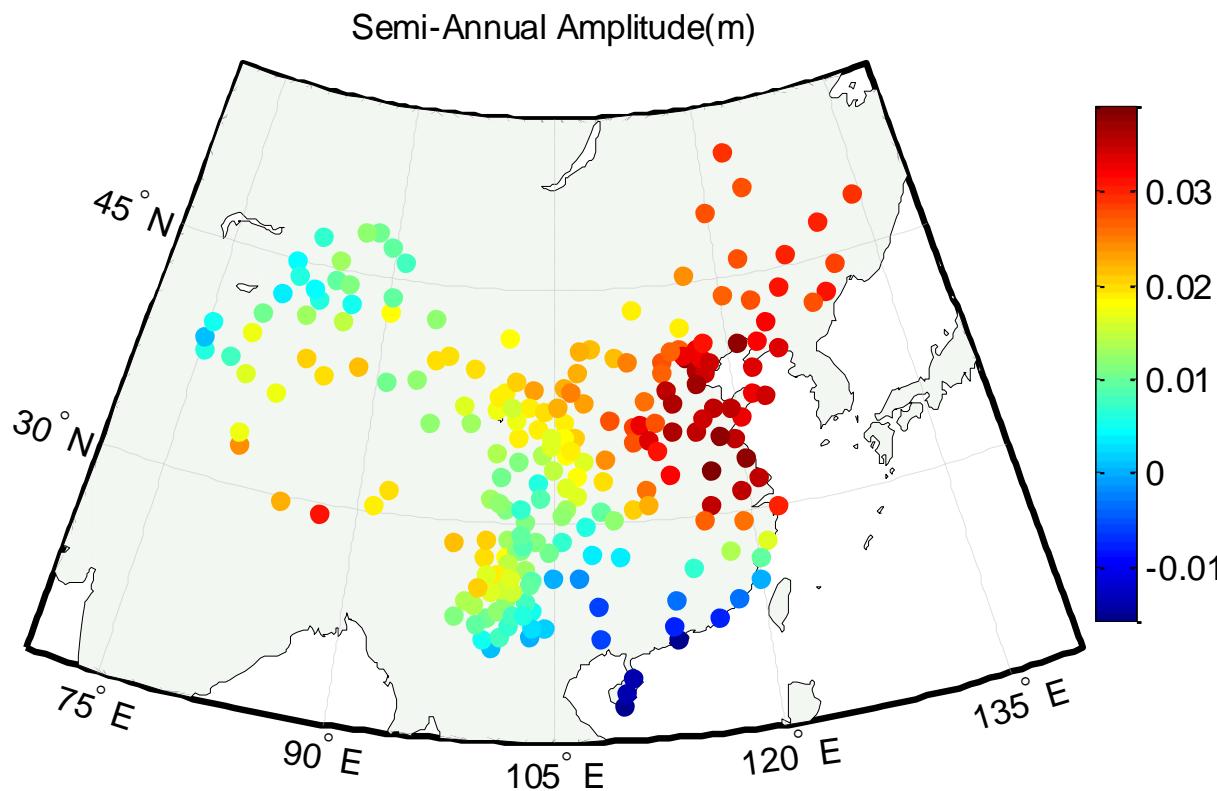
## ➤ Annual phase



# SHAtrop: ZTD semi-annual term

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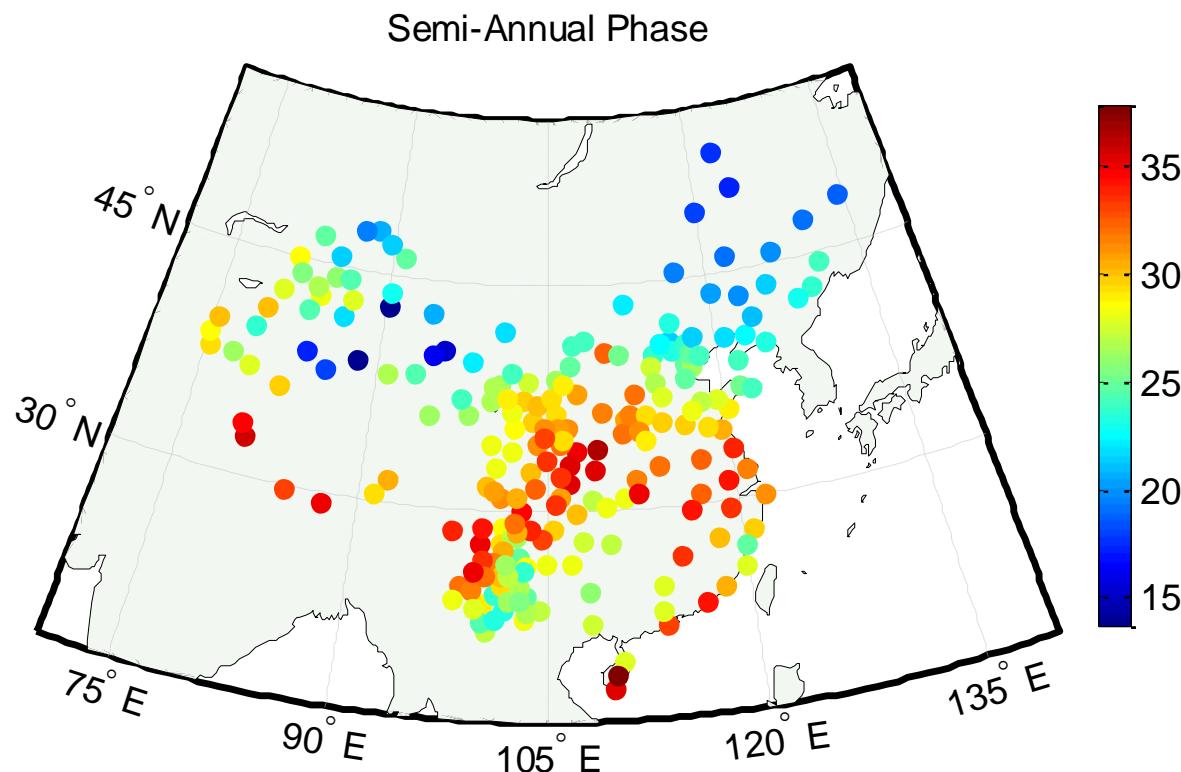
## ➤ Semi-annual amplitude



# SHAtrop: ZTD semi-annual term

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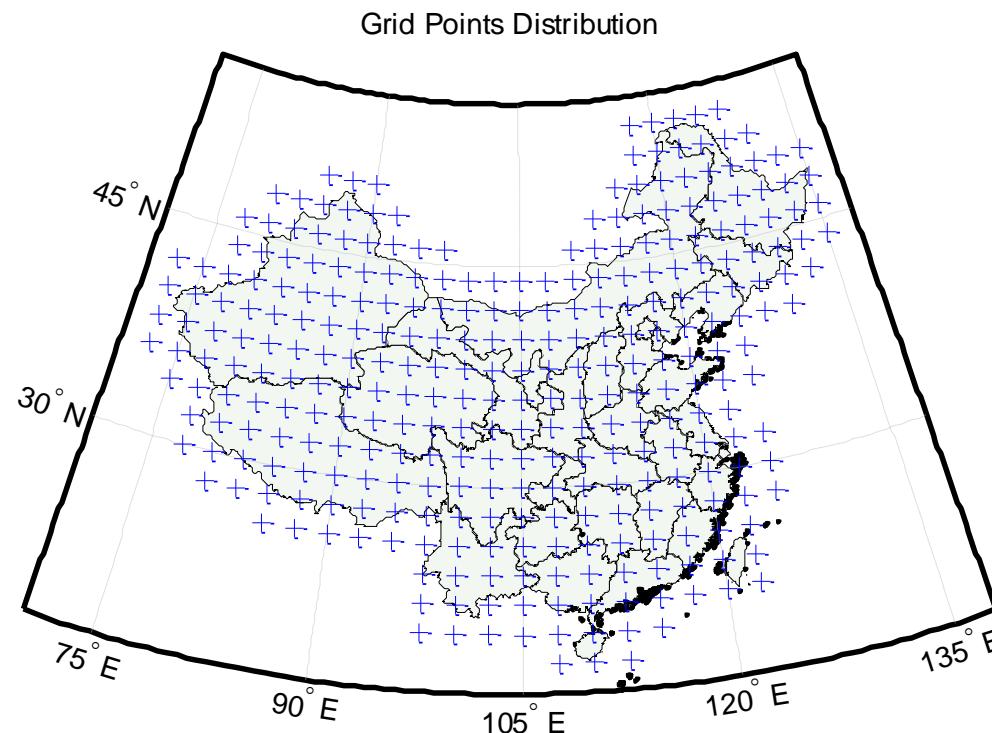
## ➤ Semi-annual phase



# SHAtrop: ZTD Grid model over China continent

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- Parameters of 152 sites
- Latitude-Longitude:  $2^\circ \times 2.5^\circ$  grid
- $[70^\circ\text{E} \sim 135^\circ\text{E}, 18^\circ\text{N} \sim 54^\circ\text{N}]$



# SHAtrop: ZTD calculation for user

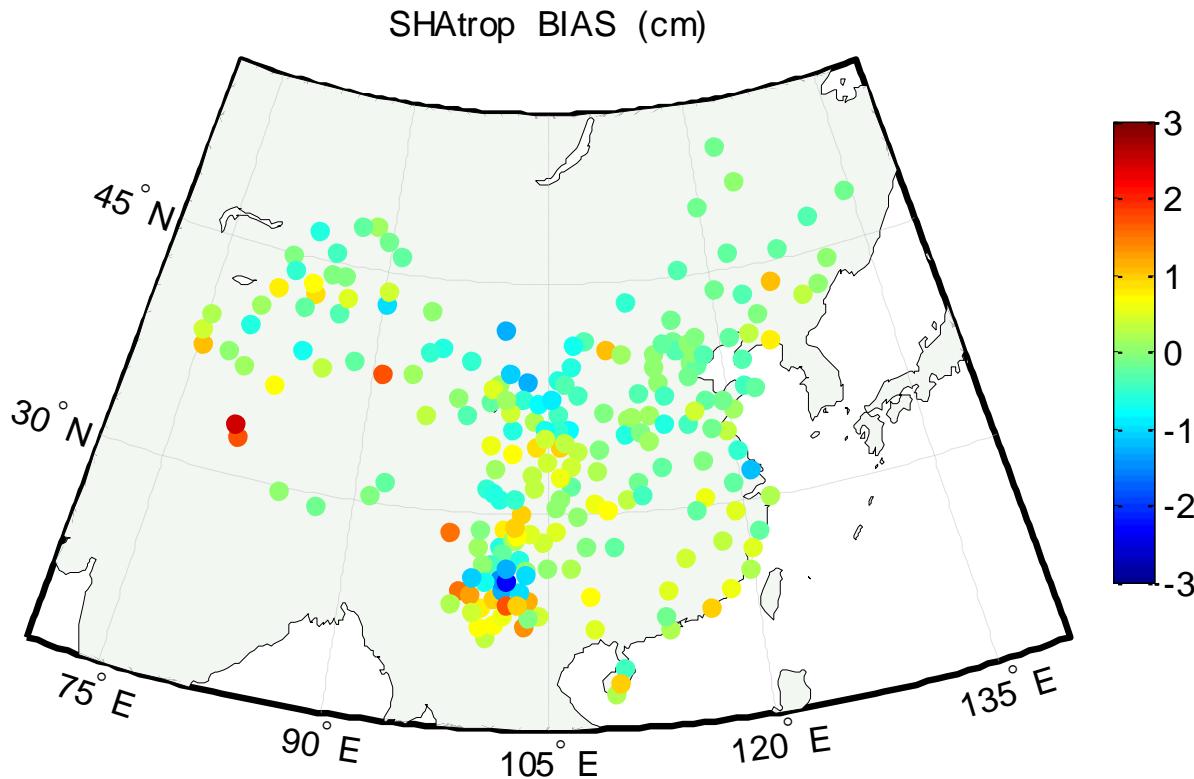
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- Select four grid points around the site
- Bilinear interpolation ( $ZTD_m$ ,  $A_1$ ,  $d_1$ ,  $A_2$ ,  $d_2$ )
- Reduction to the site height
- ZTD at each grid point is modeled by:

$$ZTD(doy, h) = \left( ZTD_m + A_1 \cos\left(\frac{2\pi}{365.25}(doy - d_1)\right) + A_2 \cos\left(\frac{4\pi}{365.25}(doy - d_2)\right) \right) \times e^{\beta h}$$

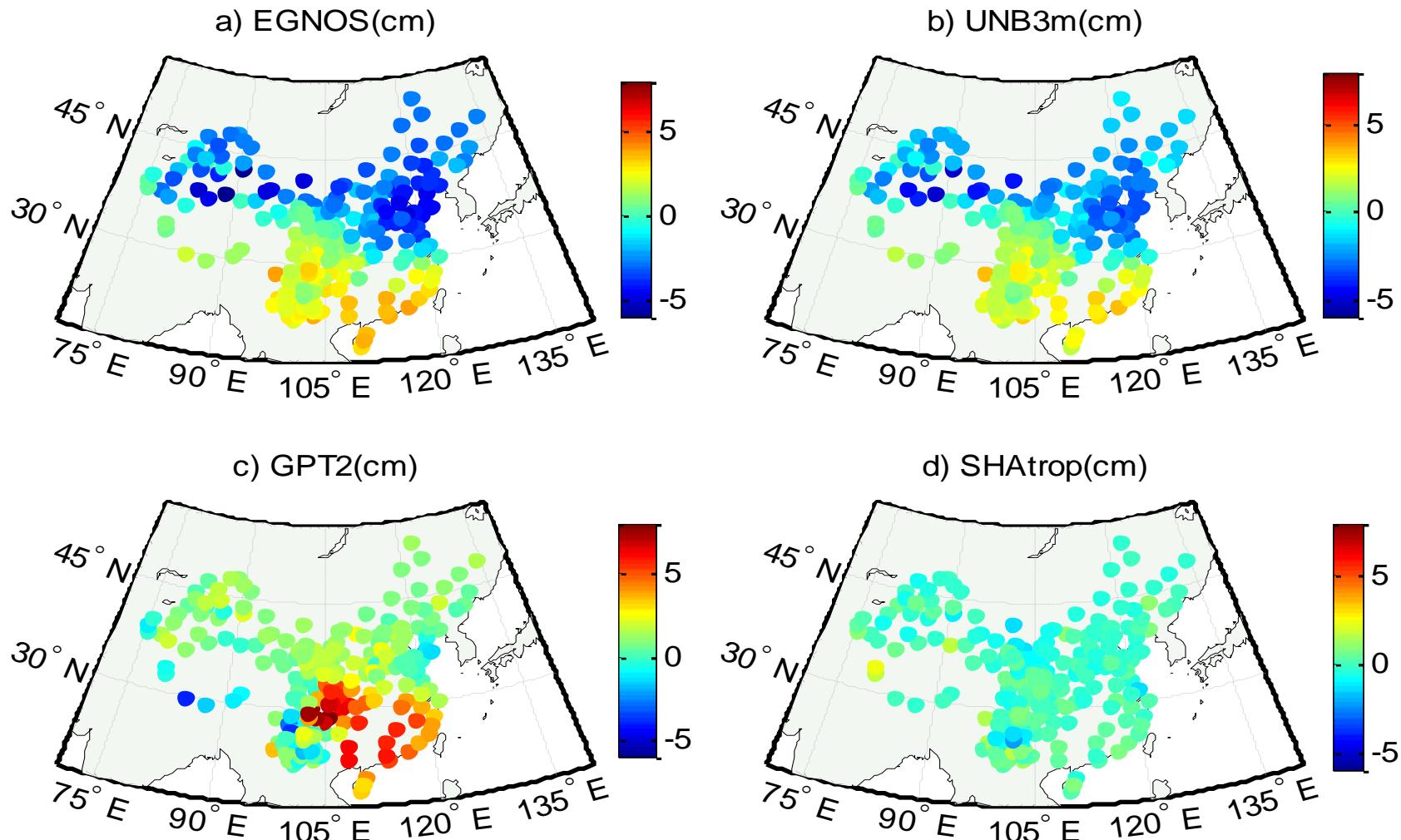
# SHAtrop: model validation - bias

- Compare to precise ZTD estimates of SHAO



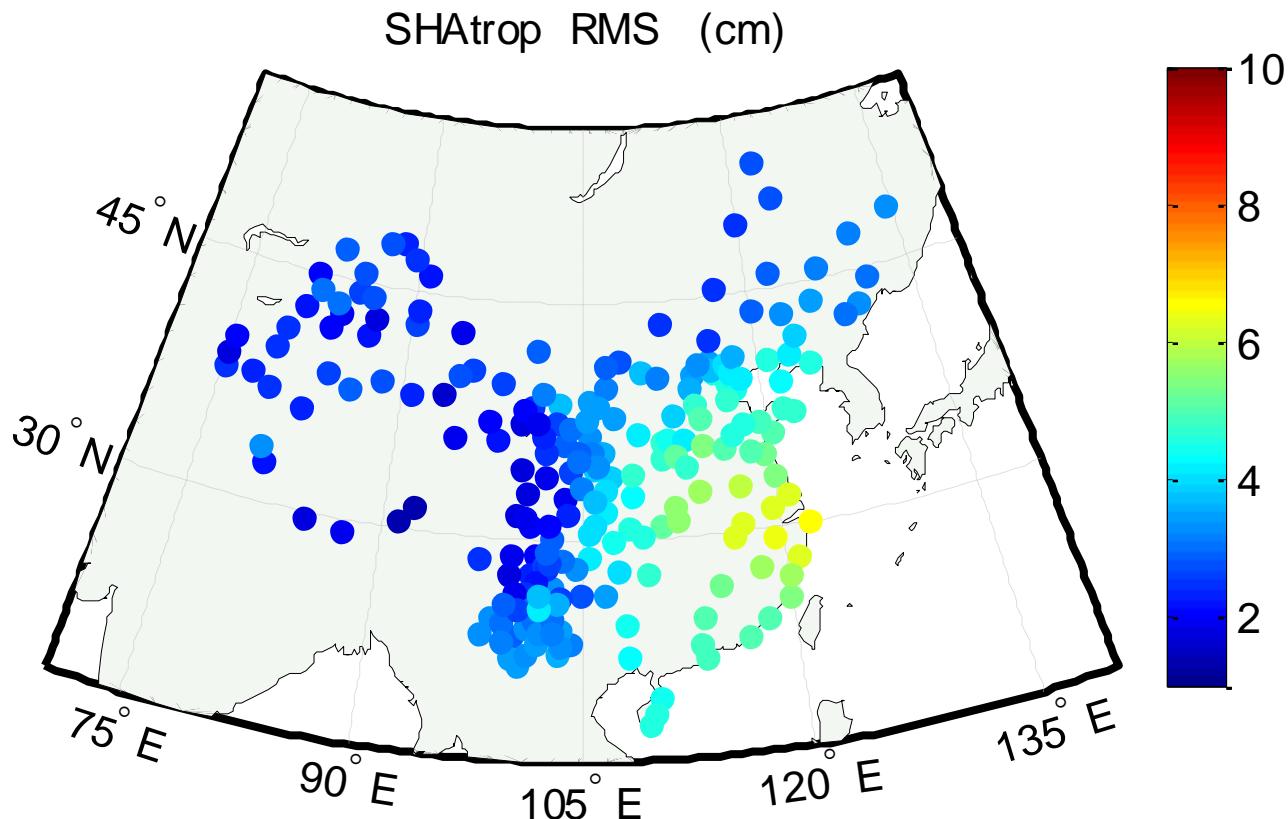
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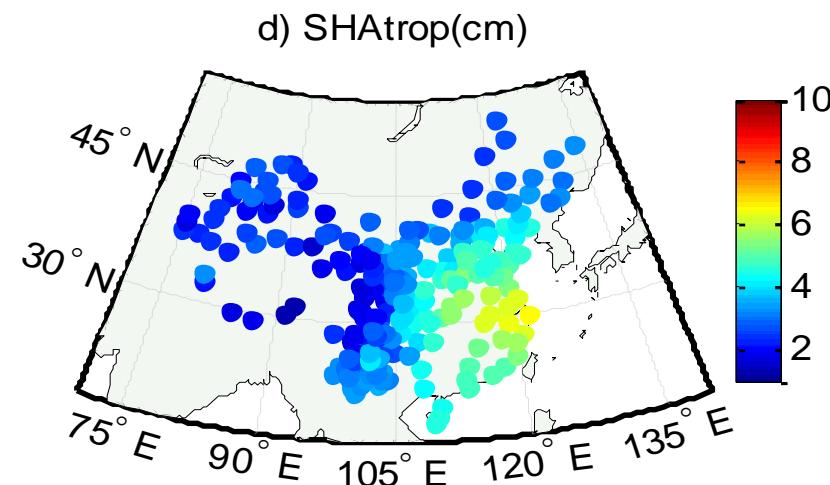
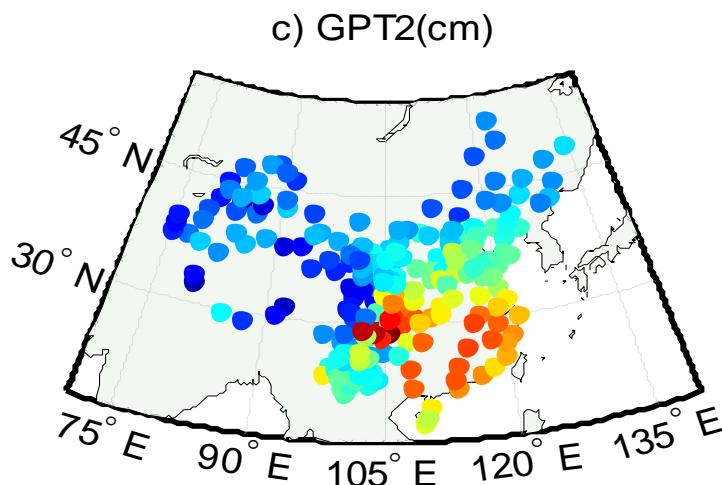
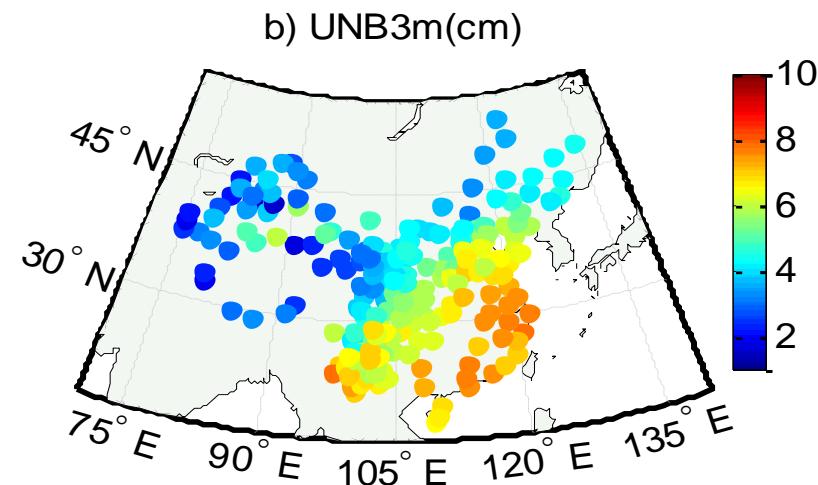
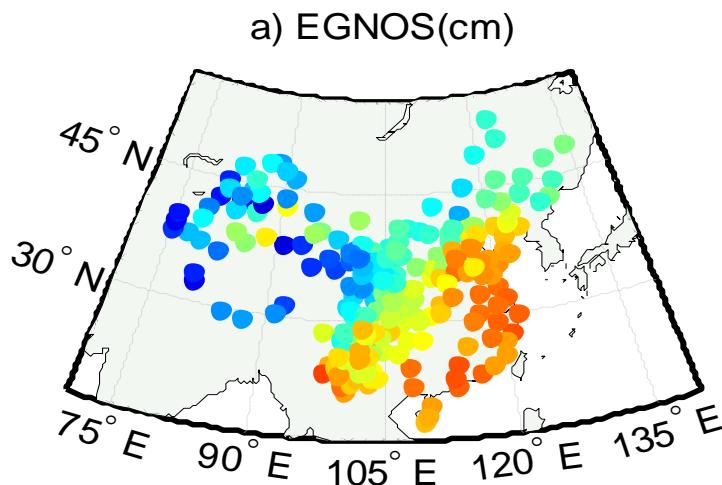
# SHAtrop: model validation - rms

➤ Compare to precise ZTD estimates of SHAO



# SHAtrop: model validation - rms

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# SHAtrop: model validation

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- Compare to precise ZTD estimates of SHAO

**Internal accuracy** using sites included in model determination

	EGNOS	UNB3m	GPT2	SHAtrop
RMS(cm)	5.64(1.77, 8.22)	5.20(1.68,7.81)	4.70(1.55,9.35)	3.45(1.34,6.56)
BIAS(cm)	- 0.58( - 5.87,3.84)	- 0.32( - 5.07,3.23)	1.67( - 3.89,7.53)	- 0.02( - 2.27,1.70)

- Improved by 39%,34%,26% over EGNOS,UNB3,GPT2

# SHAtrop: model validation

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- Compare to precise ZTD estimates of SHAO

**External accuracy** using sites not included in model determination

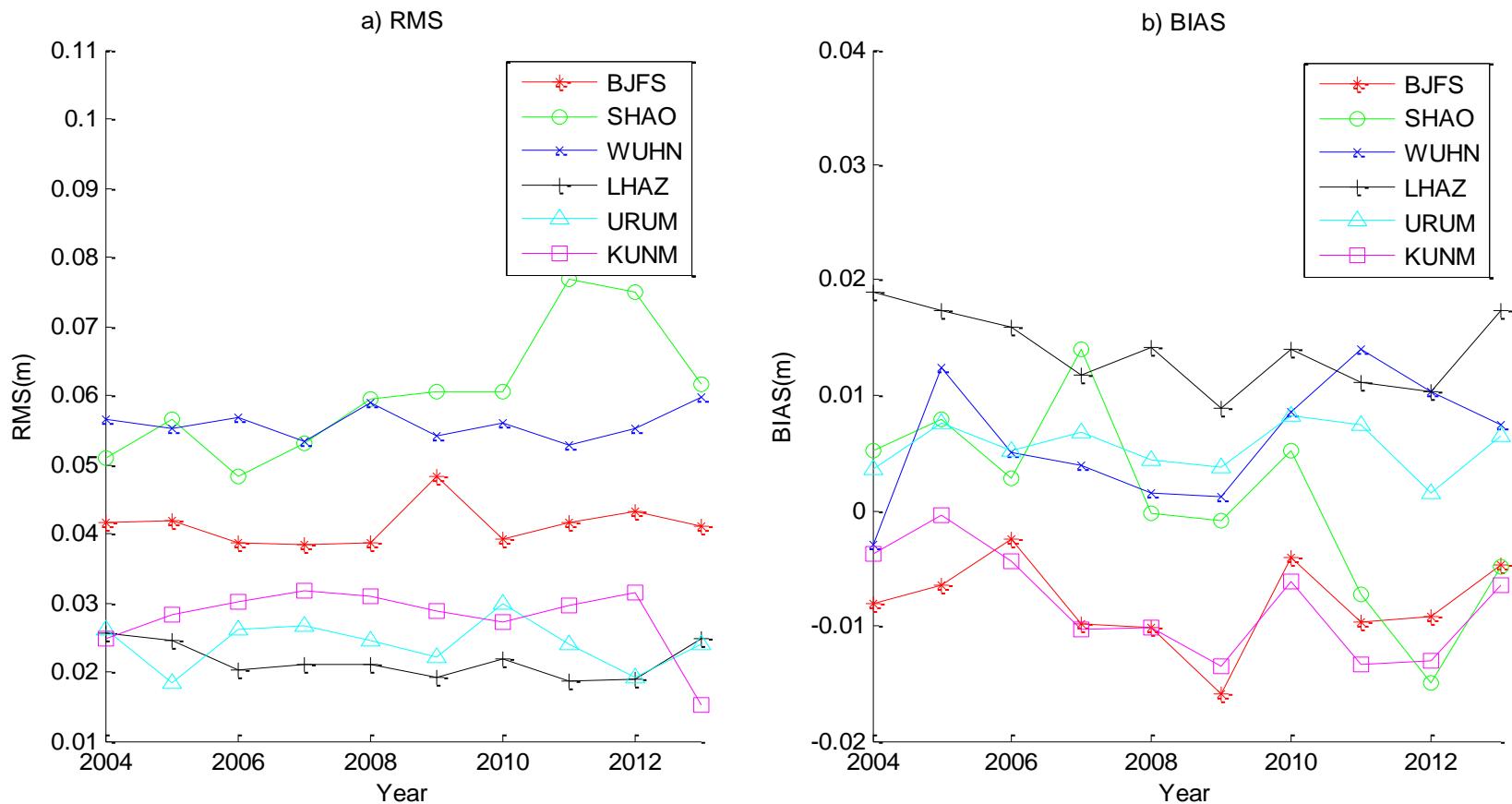
	EGNOS	UNB3m	GPT2	SHAtrop
RMS(cm)	5.45(1.75,7.89)	5.03(1.75,7.89)	4.53(1.41,10.11)	3.48(1.30,6.41)
BIAS(cm)	- 0.32( - 4.18,4.78)	- 0.08( - 3.90,3.59)	1.51( - 3.68,8.33)	0.19( - 1.31,2.51)

- Improved by 36%,31%,23% over EGNOS,UNB3,GPT2

# SHAtrop: model validation

➤ Compare to precise ZTD estimates of IGS

Long term validation: 6 IGS sites, 10 years(2004-2013)



# Summary

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- New ZTD model based on precise GNSS ZTD time series
- High spatial resolution
- Better accuracy in China continent than other empirical models

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*Acknowledgment: 863 projects  
(No. 2013AA122402,2014AA123102)  
NSFC project (No. 11273046)*

*[http://www.shao.ac.cn/shao\\_gnss\\_ac](http://www.shao.ac.cn/shao_gnss_ac)*

*Thank you!*